# Damping and Vibration Mitigation: Critical Issues

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With a little help from my friends:

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# Vibration Mitigation: Classification

- Damping Materials
- **Damping Devices**
- Isolation methods
  - (stiffness controlled) Electronic Damping

- Active Control
- Semi Active Control
- Passive Control

Here we focus on issues related to material properties, and some sense of multifunctionality



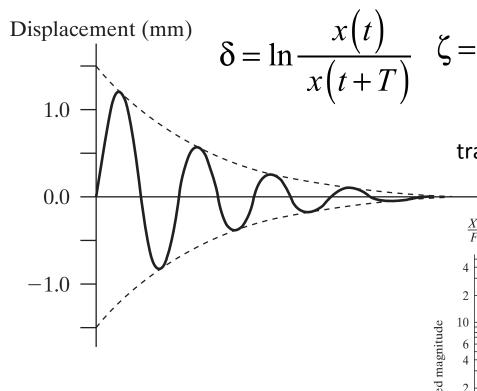
# Issues Remaining in Current State of the Art

- Damping materials typically have
  - Strong temperature dependence
  - Strong frequency dependence
  - Damping is often an add on solution rather than built in, increasing volume and mass
  - Modeling friction is a continued problem introducing nonlinearity even for small deflections
- Models of damping are difficult because of lack of first principles
- 10<sup>4</sup> Papers on in 2012 alone AEROSPACE ENGINEERING

# Why so many papers?

- Mass and stiffness, or density and elastic modulus can be measured statically
- Damping is a dynamic quantity and can only be measured by examining a dynamic response
- In many cases, intrinsic damping is small, making it even more difficult to measure
- There is no first principle, such as Hooke's law that stands up to experimental validation, from which to model damping (deformation and rate dependent)

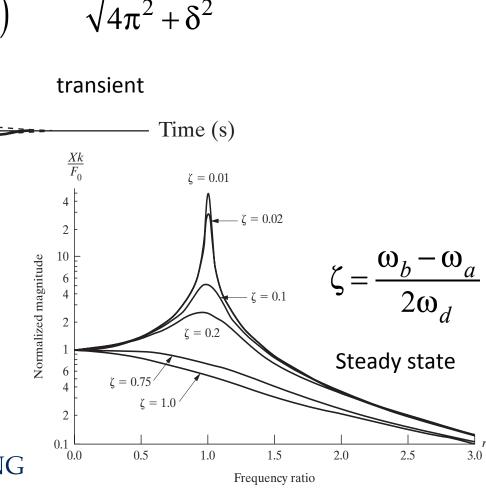
## Review of Some Basic Concepts



$$\eta = 2\zeta$$

But only at resonance!





# The Problem between Structural Models and Material Modeling

Structural models look like this

$$\frac{\partial^{2}}{\partial t^{2}}w(x,t) + \frac{EI}{\rho A}\frac{\partial^{4}}{\partial x^{4}}w(x,t) + \frac{C_{d}I}{\rho A}\frac{\partial^{5}}{\partial x^{4}}\partial t w(x,t) + \frac{C_{1}}{\rho A}\frac{\partial}{\partial t}w(x,t) = 0$$

- Which emits many modes of vibration
- Experimental coupon measurements give loss factors for each mode and a modulus, interpreted as modal damping ratios and frequencies:  $\zeta_n$ ,  $\omega_n$

Measured at coupon level

**Determined analytically** 

$$\omega_n^2 = \frac{EI}{\rho A} \beta_n^4$$
 agrees with experiental data

Measured from structural response

$$2\zeta_n \omega_n = \left| \frac{C_d I}{\rho A} \beta_n^4 + \frac{C_1}{\rho A} \right|, \text{ however:}$$

Estimates of the coefficients  $C_1$  and  $C_d$  based on modes are not consistent

1-2	0.0724	0.7092 x10 <sup>6</sup>
1-3	0.2402	0.2699
1-4	0.6053	0.0873
1-5	0.6157	0.0856
1-6	1.3901	0.0323
1-7	1.6867	0.0221
1-8	1.8039	0.0199
1-9	1.7561	0.0205

Yet, if we estimate these damping coefficients using structural measurements only, instead of coupon measurements, we can identify consistent values of  $C_d$  and  $C_1$  across different experiments and hardware



# This situation gets worse if we use a hysteretic model

**Constitutive Model** 

$$\sigma(t) = E_0 \varepsilon(\tau) + \int_0^t g(t - \tau) \frac{d\varepsilon(\tau)}{d\tau} d\tau \Rightarrow$$

Structural Model

$$\rho A \frac{\partial^2}{\partial t^2} w(x,t) + \frac{\partial^2}{\partial x^2} \left[ EIw_{xx}(x,t) - \int_{-r}^0 g(s) w_{xx}(x,t+s) ds \right] = 0$$

**Experimental Model** 

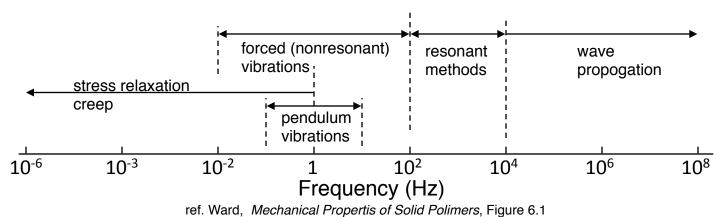
$$E' = E[1 + \eta(\omega)j]$$



$$\eta = \frac{E''}{E'} = \frac{\text{loss modulus}}{\text{storage modulus}}$$

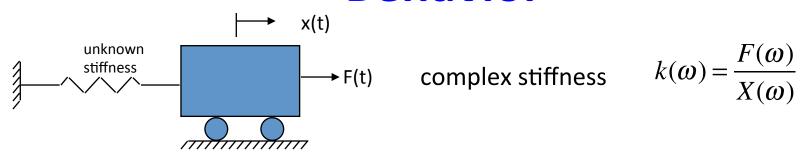
# Overview of Characterization of Damping Properties

Different approaches for different frequency ranges



- Stress relaxation/creep
  - large or small deformations measured over time
- Nonresonant testing
  - displacement due to known force measured directly
- Resonant testing
  - modulus backed out from frequency and damping of a simple structure (cantilever beam)

# Complex Stiffness Model for Viscoelastic Behavior

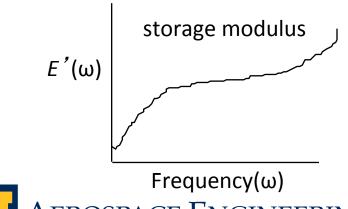


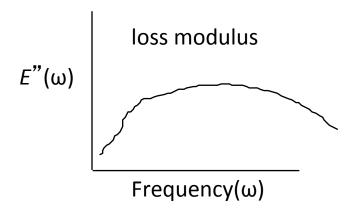
For a viscoelastic behavior the complex modulus becomes:

$$k(\omega) = E(\omega) = E'(\omega) + E''(\omega)i = E'(\omega)[1 + \eta(\omega)i]$$

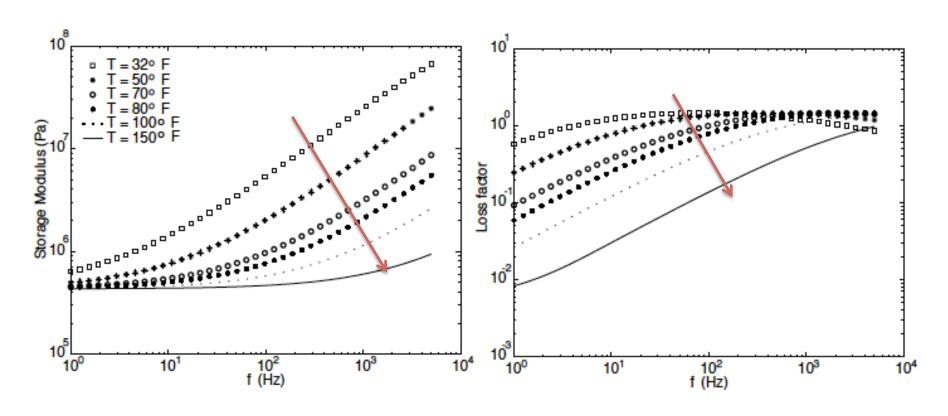
$$\tan \delta = \frac{E''}{E'} = \frac{\text{loss modulus}}{\text{storage modulus}}$$

Forming the basis of measurement schemes:





# Temperature and Frequency Dependence of a Typical Commercial Damping Material



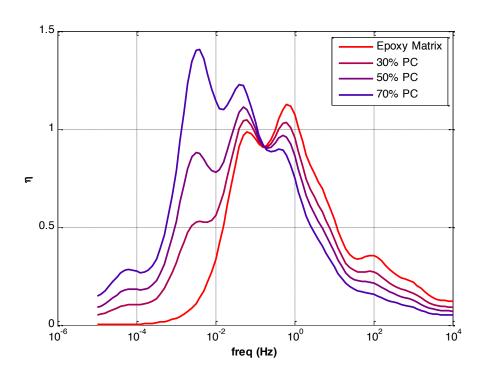
## The Major Issues

- A need for material systems and structures with uniform damping properties at harsh and extreme conditions
- Predictive macro scale models for such materials
- Predictive models of damping properties the span a range of frequencies and temperatures
- A need for multifunctional damping materials that:
  - Can be used to predict damage
  - Can heal themselves
  - That can respond to the environment
- Test apparatus capable of measuring damping at extremes
  - Frequency and temperature limit current abilities to measure properties
  - Coupon testing versus structure testing is an issue

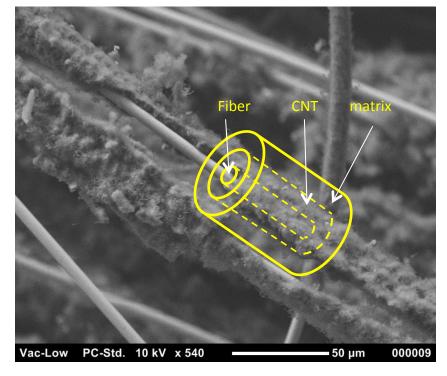
### Some Random Examples and Ideas Follow

- Infusion of nano particles to tailor damping properties
- Combining SMA with High Temperature materials
- Vascular Damping
  - Fluid induced damping
  - Particle induced damping
- Multifunctional approaches
  - Integrated with active components and sensing

# Effects of Adding Viscoelastic Particles To an Epoxy Matrix



Fuzzy fiber coated with CNT



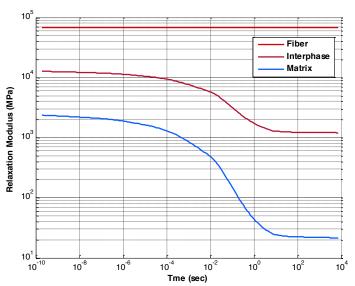
#### Sample composite analysis

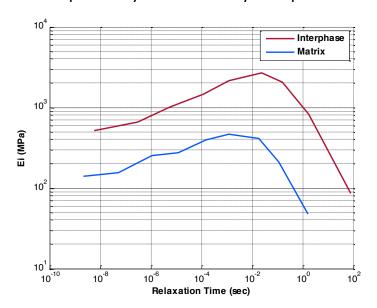
Fuzzy fiber (Glass fiber with CNT on surface)-Epoxy composite

#### **Assumptions**

- Unidirectional fibers
- Fiber diameter: 7 μ
- Interphase thickness: 5 μ
- Interpolating the relaxation functions of the fiber and matrix to obtain that of the interphase layer.

Relaxation modulus and relaxation spectrum of the interphase layer obtained by interpolation





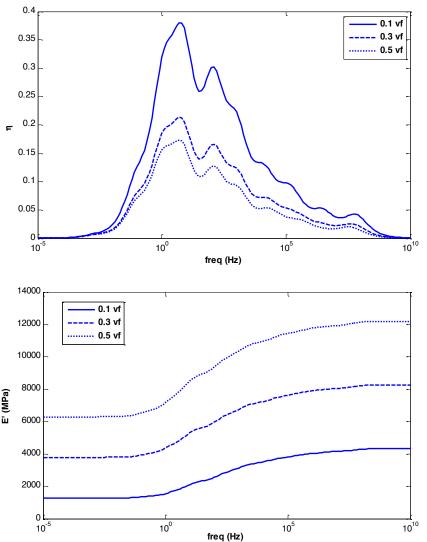


Matrix

Interphase

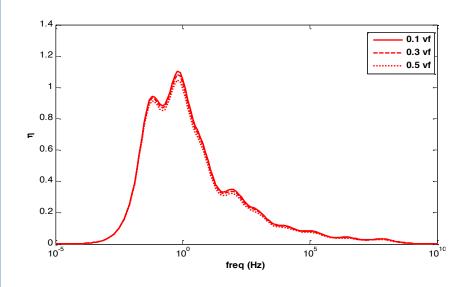
Fiber

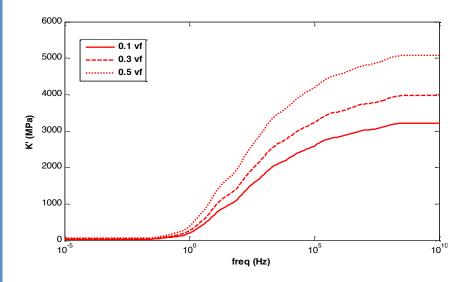
#### Axial Young's Modulus (E<sub>11</sub>)



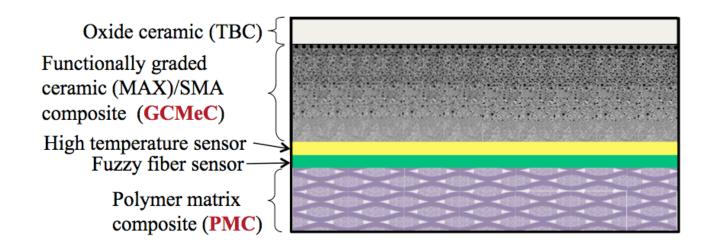
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#### In Plain Bulk Modulus (K<sub>23</sub>)





# Combining SMA with Max Phase materials to produce hybrid composites (TAM MURI/AFOSR, Stargel PM, Lagoudus, PI)



Produces unique damping and temperature properties



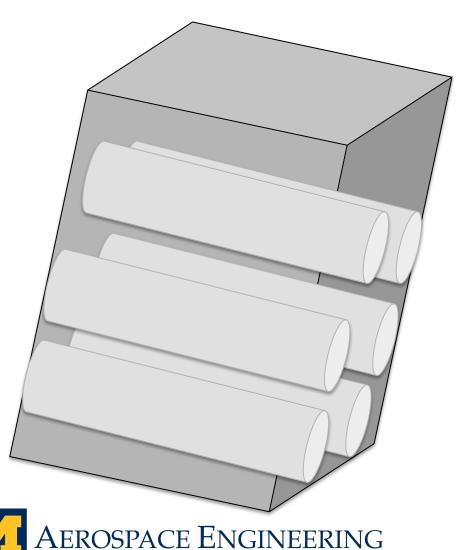
## A metric proposed by Rod Lakes

• From the material measurement point of view the  $|E*|\eta > 0.6$  GPa

for good damping properties

- Here E\* is the complex modulus
- For most materials this is only true for a narrow range of temperature near the glass transition temperature
- He uses the concept of "negative stiffness" to try and solve this problem

# **An Idea: Vascular Damping**



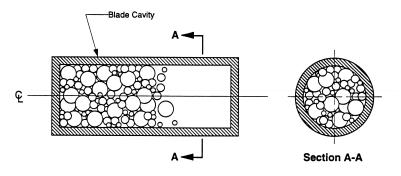
- Starting with the Vascular work of White and Sottas, add either:
  - Fluid flow to control damping
  - Or in closed cells with particles to form particle dampers

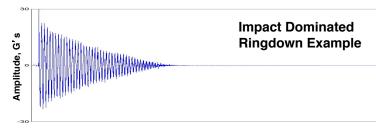


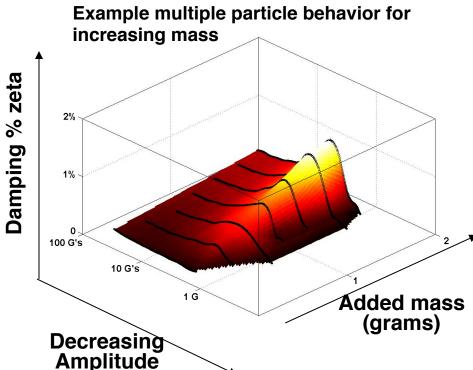
# **Particle Damping**



- Advantages
  - Broad useful temperature ranges
  - Not mode/frequency specific
  - Non-outgassing
- Variety of loss methods
  - Impact (particle-particle & particle/cavity)
  - Friction (particle-particle & particle/cavity)



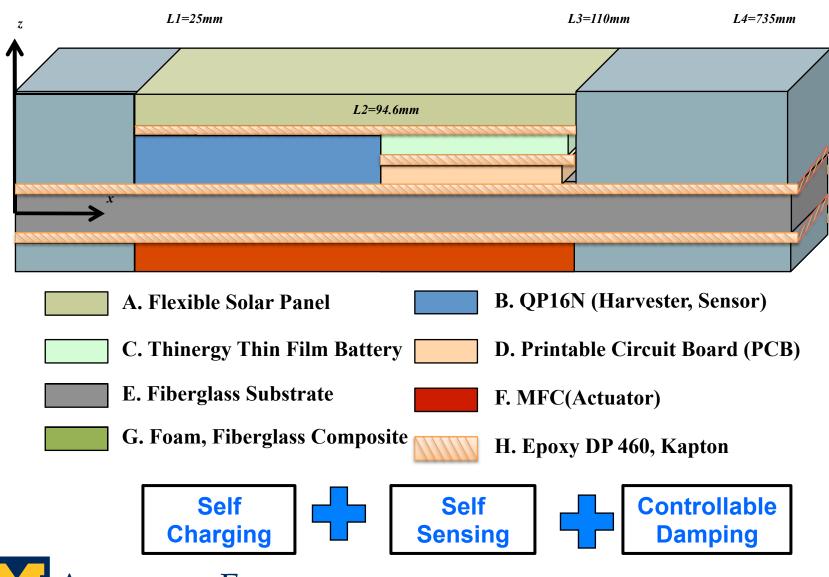




#### Caveats

- Empirical based design
- Amplitude dependent behavior
- Behavior is also dependent on cavity orientation to local quasi-static acceleration field
- Multiple other parameters can influence damping performance

#### **Electronic Damping: Multifunctional Composites**



### **Measurement Issues**

- Damping requires a dynamic load
- Usually done on coupon size materials using a frequency sweep, but the models needed are structural
- Measurements are at steady state, but transients are often of interest and the loss factor (measured) is twice the damping ratio ONLY AT RESONANCE

## Measurement and Modeling Issues are Intertwined

- In order to use material properties effectively they must be fit well into structural mechanics models
- DMA etc. measure properties in limited frequency and temperature ranges and use sine sweeps
- The values are suspect when placed into FEM codes.
- Structural codes are clumsy with hysteresis and nonlinearity

# Is there merit in using Macro Ideas at the Material level?

- Many devices are successful at the macro level:
  - Vibration absorbers
  - Vibration isolators
  - Active control
  - Magnetic (eddy current) dampers
  - MR dampers
- Can these concepts be down scaled to a multifunctional material concept?

# Is there Merit in Multi scale modeling of damping?

- Only a few papers attempted this (Liu, Wang and Bakis, 2010 for CNT nano ropes)
- Still focused on using the loss factor concept under cyclic loading
- But does have a connection between nano scale and structural scale, a first

## Why Should the Air Force Be Interested?

- Bladed disks in low and high temperature stages of jet engines are in need of damping to prevent high cycle fatigue
  - High damping at high temperatures would provide a major breakthrough in blisk designed jet engines
- Precision maneuvering of flexible space craft requires damping to control transients
  - Low temperature damping in space craft (e.g. optical payloads)
  - Damping needed to mitigate shock and vibroacoustic response in lift off
- Aeroelastic stability and sonic fatigue in aircraft
   Aerospace Engineering

## **More Potential AF Applications**

- Prevention of store induced flutter
  - Current mounts are limited in frequency range
  - Reconfiguration requires new flutter tests
  - A broad band damping material for mounts could solve this problem
- General fatigue of AF structures would be enhanced by higher damped structures

## **Summary: 3 Main Issues**

- 1. Damping materials are temperature and frequency dependent
- 2. Damping falls off in extreme environments
- 3. There is a miss match damping as seen/ measured by material engineers and structural engineers

Can multifunctional approaches solve these problems?